

Lesson 27

Factoring Trinomials of the Type $x^2 + bx + c$

Factoring $x^2 + bx + c$:

Steps to follow . . .

1. List c on the side (include the sign).
2. Find all factor pairs of c .
3. Look for a factor pair that could add or subtract to equal b .
4. Determine the signs of each number in the pair so that they add up to b and multiply to c .
5. List the factor pairs in the form $(x + \underline{\quad})(x + \underline{\quad})$.

Examples: Factor each trinomial.

$$1. \quad x^2 + 7x + 12 \quad \begin{array}{r} +12 \\ \hline 1 \quad 12 \\ 2 \quad 6 \\ +3 \quad +4 \end{array}$$

$$(x+3)(x+4)$$

$$2. \quad x^2 - 11x + 18 \quad \begin{array}{r} +18 \\ \hline 1 \quad 18 \\ -2 \quad -9 \\ 3 \quad 6 \end{array}$$

$$(x-2)(x-9)$$

$$3. \quad p^2 - 3p - 18 \quad \begin{array}{r} -18 \\ \hline 1 \quad 18 \\ 2 \quad 9 \\ +3 \quad -6 \end{array}$$

$$(p+3)(p-6)$$

$$4. \quad m^2 + 6m - 27 \quad \begin{array}{r} -27 \\ \hline 1 \quad 27 \\ -3 \quad +9 \end{array}$$

$$(m-3)(m+9)$$

$$5. \quad k^2 - 10k + 25 \quad \begin{array}{r} +25 \\ \hline 1 \quad 25 \\ -5 \quad -5 \end{array}$$

$$(k-5)(k-5)$$

$$6. \quad x^2 - 9 \quad \begin{array}{r} -9 \\ \hline 1 \quad 9 \\ -3 \quad +3 \end{array}$$

$$x^2 + 0x - 9$$

$$(x-3)(x+3)$$

$$7. \quad 4y^2 - 9$$

$$\begin{array}{c} \downarrow \quad \downarrow \\ (2y+3)(2y-3) \end{array}$$

$$8. \quad 25m^2 - 16$$

$$\begin{array}{c} \downarrow \quad \downarrow \\ (25m+4)(25m-4) \end{array}$$