

Lesson 16

Solving Systems Using Elimination

Steps to Follow: Elimination Method

- Put both equations in standard form; $Ax + By = C$
- Pick one variable to eliminate.
 - Look for variables that have the same coefficient, but opposite signs.
 - If you cannot find that, make it.
 - Look for a number that both coefficients can become (by multiplying).
 - Multiple each equation by a value that will produce the desired coefficient.
 - make sure the coefficients have opposite signs.
(If they don't, multiply one equation by negative one.)
- Add the equations together. One variable should cancel out.
- Solve the remaining equation for just the remaining variable.
- Substitute the value that you found back into one of the original equations in order to solve for the second variable.
- List your answer as an ordered pair.

Examples: Solve by Elimination

1.
$$\begin{cases} 5x - 6y = -32 & \textcircled{1} \\ 3x + 6y = 48 & \textcircled{2} \end{cases}$$

$$\begin{array}{r} 5x - 6y = -32 \\ 3x + 6y = 48 \\ \hline 8x = 16 \\ \frac{8x}{8} = \frac{16}{8} \\ x = 2 \end{array}$$

$$\begin{array}{r} \textcircled{1} \quad 5(2) - 6y = -32 \\ 10 - 6y = -32 \\ -10 \quad -10 \\ \hline -6y = -42 \\ \frac{-6y}{-6} = \frac{-42}{-6} \\ y = 7 \end{array}$$

$(2, 7)$

2.
$$\begin{cases} 2x + 5y = -22 & \textcircled{1} \cdot (-5) \\ 10x + 3y = 22 & \textcircled{2} \end{cases}$$

$$\begin{array}{r} 2x + 5y = -22 \\ 10x + 3y = 22 \\ \hline -10x - 25y = 110 \quad \textcircled{1} \\ 10x + 3y = 22 \quad \textcircled{2} \\ \hline -22y = 132 \\ \frac{-22y}{-22} = \frac{132}{-22} \\ y = -6 \end{array}$$

$$\begin{array}{r} \textcircled{2} \quad 10x + 3(-6) = 22 \\ 10x - 18 = 22 \\ +18 \quad +18 \\ \hline 10x = 40 \\ \frac{10x}{10} = \frac{40}{10} \\ x = 4 \end{array}$$

$(4, -6)$

3.
$$\begin{cases} 4x = -2y + 14 & \textcircled{1} \\ 7x - 3y = -8 & \textcircled{2} \end{cases}$$

$$\begin{array}{r} 4x = -2y + 14 \\ +2y \quad +2y \\ \hline 4x + 2y = 14 \quad \textcircled{1} \cdot (3) \\ 7x - 3y = -8 \quad \textcircled{2} \cdot (2) \\ \hline 12x + 6y = 42 \quad \textcircled{1} \\ 14x - 6y = -16 \quad \textcircled{2} \\ \hline 26x = 26 \\ \frac{26x}{26} = \frac{26}{26} \\ x = 1 \end{array}$$

$$\begin{array}{r} \textcircled{1} \quad 4x + 2y = 14 \\ 4(1) + 2y = 14 \\ 4 + 2y = 14 \\ -4 \quad -4 \\ \hline 2y = 10 \\ \frac{2y}{2} = \frac{10}{2} \\ y = 5 \end{array}$$

$(1, 5)$